

# de Sitter as a Resonance

Jonathan Maltz<sup>a,b</sup> and Leonard Susskind<sup>b</sup>

<sup>a</sup> *Center for Theoretical Physics and Department of Physics,  
University of California at Berkeley, Berkeley, CA, 94720, USA and*

<sup>b</sup> *Stanford Institute for Theoretical Physics, Stanford University, Stanford CA 94305, USA*

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A quantum mechanical formulation of de Sitter cosmological spacetimes still eludes string theory. In this paper we conjecture a potentially rigorous framework in which the status of de Sitter space is the same as that of a resonance in a scattering process. We conjecture that transition amplitudes between certain states with asymptotically supersymmetric flat vacua contain resonant poles characteristic meta-stable intermediate states. A calculation employing constrained instantons illustrates this idea.

## INTRODUCTION

The universe is not just expanding, the expansion is accelerating [1–5]. This implies that our universe is asymptotically de Sitter (dS) [6–10]. The dS metric expressed in global coordinates is

$$ds^2 = -dt^2 + l_{\text{ds}}^2 \cosh^2 \left[ \frac{t}{l_{\text{ds}}} \right] (d\psi^2 + \sin^2 \psi d\Omega_2^2) \quad (1)$$

with  $l_{\text{ds}} = \sqrt{\frac{3}{\Lambda}}$ . Expressed in conformal time

$$ds_{\text{dS}}^2 = \frac{3}{\Lambda \cos^2 \eta} \left\{ -d\eta^2 + d\psi^2 + \sin^2 \psi d\Omega_2^2 \right\} \quad (2)$$

where

$$\cosh \left[ \sqrt{\frac{\Lambda}{3}} t \right] = \frac{1}{\cos \eta} \quad (3)$$

Our current understanding of quantum gravity is dependent on the existence of stable asymptotically cold boundaries, and correlations functions evaluated at those boundaries. Supersymmetric anti de Sitter space and asymptotically Minkowski space are examples. Boundary correlators and S-matrix elements are the mathematical objects that the theory is built out of [11–15]. No such understanding exists for de Sitter space.

Even if de Sitter space were stable with respect to decay, its future spacelike asymptotic boundary would fluctuate, necessitating an integration over the geometry of future infinity—a problem which could be as complicated as any quantum gravity problem. In addition it is expected that all de Sitter vacua are unstable with respect to Coleman De Luccia (CDL) decay to flat and AdS vacua [16, 17]. This would further complicate the asymptotic future boundary, turning it into a superposition of fractals populated by crunches and hats.

But the existence of hats—FRW patches with vanishing cosmological constant—create a new opportunity for a rigorous framework for de Sitter space, in which it appears as a metastable state in a transition amplitude between two asymptotically flat states. Our purpose in this

paper is to define such a transition amplitude and show that resonant poles, associated with de Sitter intermediate states, exist in its spectral representation.

To illustrate the idea we begin with a configuration that resembles a time-symmetric slice of a de Sitter vacuum. The state can be propagated forward and backward in time to give past and future quantum superpositions of fractal boundaries, each containing an infinite number of hats. We make a gauge choice by picking a hat in the past and a hat in the future and transform them to the center of a causal diamond. The causal diamond of the hats comprise a universe for an observer who begins and ends in the past and future hats.

The complete details of the computation will be presented in a technical paper that one of us will publish concurrently [18]. Suggestions that dS might be viewed as a resonance have occurred previously [19], however there has been to the authors' knowledge no calculation to establish this. We present one in this work.

## RESONANCES AND THE CAUSAL PATCH

In [19] a simplified landscape of two minima, one with  $\Lambda > 0$  and the other with  $\Lambda = 0$  was considered and an  $O(D-1)$  symmetric CDL instanton solution was worked out; the Penrose diagram for this spacetime is the left diagram of Fig. 1. On the spacelike slice in the middle of the left diagram of Fig. 1 a Hartle Hawking state for the spacetime can be constructed and evolved to an *Out* state [20]. The information within the causal patch (Regions *I* + *II* + *III*) is then all that is needed to capture all the information if Horizon Complementarity [21–24] is correct, as anything that passes out of the causal patch (goes into *IV*) will have a complementary description in terms of the highly scrambled Hawking radiation which will go into *I*. Therefore a spacelike slice in *I* will contain all the information from the Hartle-Hawking state and we can construct the *Out* state there [25].

A resonance is an intermediate meta-stable state which can occur between any pair of initial and final states [26]. Many of these channels can be used to establish the ex-

istence of a resonance. We compute a spectral representation of the transition amplitude between *In* and *Out* states,  $\langle Out|In \rangle$ , and show that it contains a pole characteristic of a dS intermediate state [27, 28]. The location of the pole is a function of  $\Lambda$ .

The transition is computed as a path integral over all histories – including all possible spacetime configurations, and field configurations – that connect the *In* and *Out* states. A mathematically tractable, though not realistic channel, as it is entropically suppressed, is to construct the *In* and *Out* states by evolving in a time reversal symmetric manner from a semi-classical spacelike slice in the middle of *III*. We are not proposing that this is the true cosmological history of our universe, we are proposing that such a pole in such an amplitude provides a precise definition within the context of supersymmetric backgrounds of a dS space [29]. This is the same logic that applies to any meta-stable state in quantum mechanics.

Consider the CDL instanton in the thin wall tensionless domain wall limit (See Center Diagram Fig.1) which can be constructed using Barrabès-Israel Null junctions conditions [30]. The details of the nucleation process are not important in what follows.

We will define the amplitude as a path integral over the causal patch containing the hats. We will not try to justify this; we will define such an amplitude to be the object of interest and show that it has a dS pole in the spectral representation. This definition eliminates the complicated fractal boundaries in region *IV* and *V*.

An off shell continuation of this configuration has the nucleation point and its time reversal separated by a finite conformal time  $2\eta_0$  (See the right diagram of Fig.1). In what follows we will truncate the path integral to an integral over  $\eta_0$ , (4). This deformed spacetime is not a true instanton of the original CDL equations but has the status of a constrained instanton solution [31–33], with the constraint that the separate the FRW regions are separated by a given proper time along geodesic  $\psi = 0$ . We will refer to this spacetime as the *constrained* CDL instanton. The path integral over histories (4) will contain deformations of this geometry including metric and field fluctuations about the instanton solution as well as non-perturbative effects such as further vacuum decay outside the hat. This mini-superspace approximation allows us focus on the first contribution to this path integral over all histories of the metric and fields (4) by only integrating over histories where no particle content is excited and the integration  $\eta_0$ . Defining the proper-time along  $\psi = 0$  to be  $2t_0$  using (3),

$$\begin{aligned} \langle Out|In \rangle &= \int \mathcal{D}g \mathcal{D}\varphi \exp \{i S[g, \varphi]\} \\ &\sim \mathcal{N} \int dt_0 \exp \{i S[t_0]\} + \text{Higher order terms.} \end{aligned} \quad (4)$$

This expresses the amplitude as an integral over the

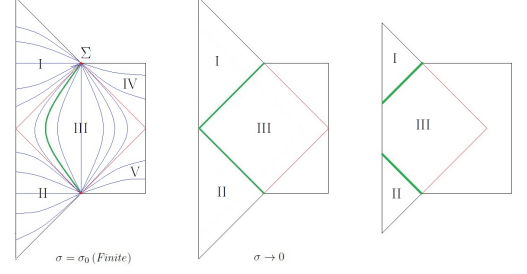


FIG. 1. (Left) The Penrose diagram of the Lorentzian continuation of CDL instanton solution [19, 34, 35]. *I* and *II* are an open ( $k = -1$ ) FRW universes which are asymptotically flat [19, 34, 35]. *IV* and *V* are asymptotically dS.  $\Sigma$  is the conformal 2-sphere defined by the intersection of the lightlike infinity of *I* and the spacelike infinity of *IV*. The curves indicate orbits of the  $SO(3, 1)$  symmetry, which as the conformal group on  $\Sigma$  [35]. The red lines between *III*, *IV*, and *V* represent the cosmological horizons in the dS of the observer at  $r = 0$ . The green curve in *III* represents the domain wall between the FRW and dS regions. (Center) The tensionless domain wall limit (Right) the Constrained CDL spacetime where the FRW bubbles are separated by  $2\eta_0$ , here *III* is pure dS and is the unregulated integration region.

relative time between the initial and final hats. The Fourier transform of the  $t_0$  dependence defines the spectral representation of  $\langle Out|In \rangle$ .

## THE ACTION IN LIOUVILLE GRAVITY

In this section we will illustrate the computation in the context of  $dS_2$  which can be described by lorentzian timelike Liouville quantum gravity [36–39] which has  $dS_2$  as a solution [39–41]. The action will have bulk contributions and Gibbons-Hawking boundary contributions from the causal patch. In  $1 + 1$  dimensions, the Gauss-Bonnet theorem implies that the boundary contributions integrate to the Euler Characteristic of the geometry; therefore in  $1 + 1D$  we only need to consider the volume contribution to the action  $S[\eta_0]$ . In the approximations that we are employing the only contributions to the action  $S[\eta_0]$  that are  $\eta_0$  dependent are those of the purely dS region [42], the shaded portion of Fig. 2(a). Gauge fixing the metric using conformal gauge  $g_{\mu\nu} = e^{\phi_c} \eta_{\mu\nu}$  gives the liouville action,  $S_L[\eta_0] = -\frac{1}{16\pi b^2} \int d^2\xi (\eta^{ab} \partial_a \phi_c \partial_b \phi_c - 16\lambda e^{\phi_c})$  with  $e^{\phi_c} = \frac{3}{\Lambda \cos^2 \eta}$  and  $\lambda = \pi \mu b^2$  so  $\frac{1}{2\pi b^2} = \frac{\pi \mu}{2\pi \lambda} = \frac{4\mu}{4\Lambda}$ , [43]. The action must be regulated as it is IR divergent due to the infinite volume in the tips near future and past infinity. The regulator must be one that respects the dS and Lorentz boost symmetries [44] in order to separate the divergence in an invariant way. Surfaces of constant  $r_0^2 = \frac{3 \sin^2 \psi}{\Lambda \cos^2 \eta}$  will serve as a cutoff. (In higher dimensions

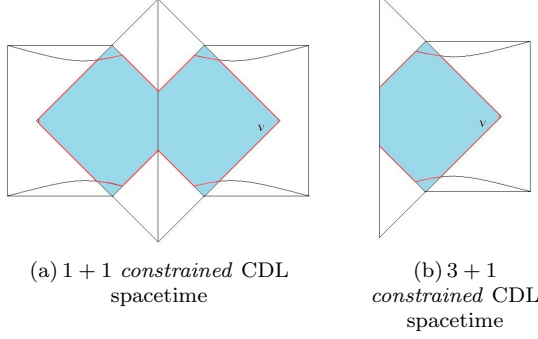


FIG. 2. (a) The slices of constant  $r_0^2 = \frac{3 \sin^2 \psi}{\Lambda \cos^2 \eta}$  are the curved surfaces intersecting the null lines at  $\psi_1 = \arctan \left[ \frac{\cos [\eta_0]}{\sin \eta_0 + \sqrt{\frac{3}{\Lambda r_0^2}}} \right]$  and  $\psi_2 = \frac{\pi}{2} - \arctan \left[ \frac{\sin \eta_0 - \sqrt{\frac{3}{\Lambda r_0^2}}}{\cos \eta_0} \right]$  as well as their reflection about  $\psi = 0$ . The null domain walls dividing the dS and FRW regions intersect  $\psi = 0$  at conformal time  $\eta = \eta_0$  and  $\eta = -\eta_0$ . (b)  $\mathcal{V}$  for the 3 + 1 space time.

these are surfaces of constant transverse  $\mathbb{S}^{d-1}$  radius in  $d + 1$  dimensions.) Spacetime points move along these surfaces under boosts and rotations. The regulated integration region is the section bounded by the red curve in Fig. 2(a),  $\mathcal{V}$ .

Evaluating  $-\frac{1}{16\pi b^2} \int_{\mathcal{V}} d^2 \xi \{ \eta^{ab} \partial_a \phi_c \partial_b \phi_c - 16\lambda e^{\phi_c} \} = \frac{1}{4\pi b^2} \int_{\mathcal{V}} d\psi d\eta \frac{1 + \sin^2 \eta}{\cos^2 \eta}$ , and expanding it in a Laurent expansion in  $w_0 = 1/r_0$  up to  $O[w_0]$ , yields,

$$S_L = \frac{-4 \log \left| \sqrt{\frac{3}{\Lambda}} w_0 \right| + 4 - \frac{\pi^2}{4} + \frac{\eta_0^2}{2} - 2 \log \cos \eta_0}{\pi b^2}, \quad (5)$$

with  $\frac{1}{\pi b^2} = \frac{4! \mu}{2\Lambda}$ . The  $-\frac{4! \mu}{2\Lambda} \{ \log \sqrt{\frac{3}{\Lambda}} w_0 - 4 + \frac{\pi^2}{4} \}$  term is the divergent contribution of the action which remains when  $\eta_0 = 0$ . It is just the action of the lorentzian tensionless domain wall CDL instanton,  $S_0$ , in this limit, and when exponentiated can be absorbed into the overall normalization factor of (4). Expressing (5) in terms of proper time  $t_0$  and defining  $\tilde{S}_L = S_L - S_0$ , up to  $O[w_0]$ ,

$$\tilde{S}_L = \frac{4! \mu}{4\Lambda} \left\{ \arctan^2 \left[ \tanh \left[ \sqrt{\frac{\Lambda}{3}} t_0 \right] \right] + \log \cosh \left[ \sqrt{\frac{\Lambda}{3}} t_0 \right] \right\}. \quad (6)$$

The only term which grows with  $t_0$  is  $\log \cosh \left[ \sqrt{\frac{\Lambda}{3}} t_0 \right] = \sqrt{\frac{\Lambda}{3}} t_0 + \log |1 + e^{-2\sqrt{\frac{\Lambda}{3}} t_0}| - \log 2$ , the others are bounded. Thus we find for large  $t_0$ ,  $\tilde{S}$  behaves like  $\sqrt{\frac{\Lambda}{3}} t_0$ . Treating bounded term as a perturbation and fourier transforming with respect to  $t_0$  yields,

$$\begin{aligned} \int_0^\infty dt_0 e^{i(\tilde{S}_L[t_0] - \omega t_0)} &= \int_0^\infty dt_0 e^{i(2\mu\sqrt{\frac{3}{\Lambda}} t_0 - \omega t_0)} + \dots \\ &= \frac{i}{\omega - 2\mu\sqrt{\frac{3}{\Lambda}}} + \rho_1[\omega] + \dots, \quad (7) \end{aligned}$$

thus revealing a pole in the spectral representation. One notes that,  $2\mu\sqrt{\frac{3}{\Lambda}}$ , is the energy of the static patch of dS, we take the existence of this pole to the indication of an intermediate dS vacuum.

This indicates that that the dS can be thought of as a resonance in a transition amplitude.

The pole in (7) occurs at a real value of  $\omega$  but this is an approximation. When the meta-stable character of the dS vacuum is accounted for the cosmological constant will obtain a small imaginary part determined by the CDL decay rate. This will shift pole by a slightly imaginary amount, which is standard in the analysis of resonances [28, 45].

## THE 4 DIMENSIONAL CASE

Lets repeat this in 3 + 1 D using the GR limit of the spacetime [46]. The regulated cutoff region  $\mathcal{V}$  is shown in Fig. 2(b).  $\mathcal{V}$  is bounded by spacelike and null surfaces. Hence we must append to the Einstein-Hilbert action [47] the Gibbons-Hawking-York boundary term [48, 49]. The boundary term has to be generalized to null surfaces and corners as in [50–54][55].

$$\begin{aligned} S &= \int_{\mathcal{V}} \frac{d^4 x}{2\kappa} \sqrt{-g} (R - 2\Lambda) - \sum_{i=2,4,6} \int_{\partial \mathcal{V}_i} d^3 x \frac{\sqrt{h_{(i)}} K_{(i)}}{\kappa} \\ &+ \sum_{i=1,3,5,7} \frac{1}{2\kappa} \int_{\partial \mathcal{V}_i} d^2 x \sqrt{q_{(i)}} \Theta + \sum_{j=1}^5 S_{\text{corner},(j)}. \quad (8) \end{aligned}$$

The second to last term is the null surface contribution and the last term is the five corner contributions which depend on a product of their boost angle and the area of the  $\mathbb{S}^2$  at that point [52, 54]. The geometry is closely related to wick rotations of those in [52–54, 56] where the analysis of the null and corner terms was carried out. More detailed arguments on these terms will be given in [18].

Evaluating (8) to  $O[w_0]$ , with  $w_0 = 1/r_0$  and as a function of  $t_0$ , gives

$$\begin{aligned} S &= \frac{4\pi 4!}{2\kappa \Lambda} \left\{ \frac{1}{2} \log \cosh \left[ \sqrt{\frac{\Lambda}{3}} t_0 \right] + \frac{1 - \sinh^2 \left[ \sqrt{\frac{\Lambda}{3}} t_0 \right]}{8 \cosh^2 \left[ \sqrt{\frac{\Lambda}{3}} t_0 \right]} \right. \\ &\left. + \left\{ \frac{1}{4} - \log 4 \right\} \tanh^2 \left[ \sqrt{\frac{\Lambda}{3}} t_0 \right] \right\} + S_0, \quad (9) \end{aligned}$$

with  $S_0 = \frac{4\pi 4!}{2\kappa\Lambda} \left\{ \frac{\Lambda}{2w_0^2} + \frac{1}{2} \log \frac{\Lambda}{3w_0^2} + \frac{5}{24} \right\} + S_{\text{corner}}$  containing divergent terms which are  $t_0$ . Apart from the  $\log \cosh \left[ \sqrt{\frac{\Lambda}{3}} t_0 \right]$  term the  $t_0$  dependent terms of (9) are bounded and monotonic for  $t_0 > 0$ . Fourier transforming the amplitude with  $\tilde{S} = S - S_0$  and employing a similar expansion as (7) reveals the pole again,

$$\begin{aligned} \int_0^\infty dt_0 e^{i(\tilde{S}[t_0] - \omega t_0)} &= \int_0^\infty dt_0 e^{i(2\frac{4\pi}{\kappa} \sqrt{\frac{3}{\Lambda}} t_0 - \omega t_0)} + \dots \\ &= \frac{i}{\omega - 2\frac{4\pi}{\kappa} \sqrt{\frac{3}{\Lambda}}} + \dots \end{aligned} \quad (10)$$

Again we have a pole in the spectral representation at the energy of the static patch. This term will be present in  $d + 1$  dimensions.

## DISCUSSION AND CONCLUSIONS

The main implication of this paper is: There exist transition amplitudes between supersymmetric flat vacua employed in string theory, that possess dS vacua as resonances. Although we have not mentioned it a given dS vacuum contains an exponentially large number of almost degenerate states and in a real quantum theory we would expect a correspondingly dense collection of poles. This is analogous to the idea of a black hole as a collection of resonances.

None of this should be taken to mean that ordinary scattering amplitudes for finite numbers of particles contain dS. The  $|In\rangle$  and  $|Out\rangle$  states we are discussing are open ( $k=-1$ ) FRW cosmologies which contain an infinite number of particles. The particles are uniformly distributed on hyperbolic surfaces and particular there exists an infinite number of particles on  $\Sigma$  of Fig. 1(Left).

We suggest that states of this type form a superselection sector in which the dS resonances are found. Since these states contain an infinite number particles but their entropy must not exceed the finite dS entropy of the causal patch, they must be infinitely fine tuned. Such states would be the bulk states of FRW/CFT [19, 35, 57, 58] or similar string theory construction that possesses dS as an intermediate configuration.

It has been asked how recent work on complexity and relations between geometry and entanglement apply in a cosmological setting. In  $2 + 1$  D the action calculation when continued to AdS is similar to wick rotated calculations relating complexity to action in the AdS BTZ black hole [53, 56]. In the continuation  $\mathcal{V}$  replaces the Wheeler DeWitt patch of [53, 56]. In both cases the action grows linearly with time  $t_0$ , which in the dS case leads to the resonant pole found, in the AdS version it represents the linear growth in complexity. It is possible that in cosmology the exponential expansion of space

may also represent a growth in complexity; further study in this direction is demanded.

A longer paper containing details of the computation will be released concurrently [18].

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